## USN

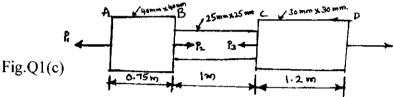
## Third Semester B.E. Degree Examination, June / July 2014 Mechanics of Materials

Time: 3 hrs. Max. Marks:100

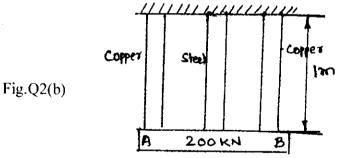
Note: Answer any FIVE full questions, selecting atleast TWO questions from each part.

## PART - A

- 1 a. Define i) Poisson's ratio ii) Bulk modulus iii) Factor of safety iv) Principle of super position. (04 Marks)
  - b. Distinguish between a ductile materials and a brittle material. Give one example each. Draw typical stress strain diagram for each of them indicating salient points on them. (08 Marks)
  - c. A member ABCD is subjected to point loads  $P_1$ ,  $P_2$ ,  $P_3$  and  $P_4$  as shown in fig.Q1(c). Calculate the force  $P_3$  necessary for equilibrium, if  $P_1 = 120 \mathrm{kN}$ ,  $P_2 = 220 \mathrm{kN}$  and  $P_4 = 160 \mathrm{kN}$ . Determine also the net change in the length of the member. Take  $E = 200 \mathrm{GN/m^2}$ .



- 2 a. Establish a relationship between the modulus of elasticity and modulus of rigidity. (10 Marks)
  - b. A horizontal rigid bar AB weighing 200kN is hung by three vertical rods, each of 1m length and 500mm² in cross section as shown in fig.Q2(b). The central rod is of steel and the outer rods are of copper. If the temp rise is  $40^{\circ}$ C. Estimate the load carried by each rod and how much the load will descend. Take  $E_s = 200 \text{GN/m}^2$ ,  $E_c = 100 \text{GN/m}^2$ ,  $\alpha_s = 1.2 \times 10^{-5}/^{\circ}$ C. (10 Marks)



- a. Show that: i) Sum of normal stresses in any two mutually perpendicular direction is constant. ii) Principle planes are planes of maximum normal stress also. (10 Marks)
  - b. At a point in a strained material, there is tensile stress of 80N/mm² upon a horizontal plane and compressive stress of 40N/mm² upon a vertical plane. There is also a shear stress of 48N/mm² upon each of these planes. Determine the planes of maximum shear stress at the point. Determine also the resultant stress on the planes of maximum shear stress. (10 Marks)
- 4 a. Derive the expression for circumferential and radial stresses in the wall of thick cylinder (Lame's equation). (10 Marks)

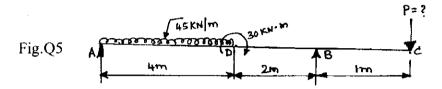
b. Determine the maximum and minimum hoop stress across the section of a pipe of 400mm internal diameter and 100mm thick, when the pipe contains a fluid at a pressure of 8N/mm<sup>2</sup>. Also sketch the radial pressure distribution and hoop stress distribution across the section.

(10 Marks)

PART - B

For the beam AC shown in fig.Q5(a), determine the magnitude of the load P acting at C, such that the reaction at supports A and B are equal. Draw SF and BM diagrams for the beam. Mark the salient points and their values on the diagram. Locate the point of contraflexure, if any.

(20 Marks)



- a. Prove that the ratio of depth of width of the strongest beam that can be cut from a circular 6 log of diameter 'd' is 1.414. Hence calculate the depth and width of the strongest beam that can be cut of cylindrical log of wood whose diameter is 300mm.
  - b. Prove that in case of a rectangular section of a beam, the maximum shear stress is 1.5 times average shear stress. (10 Marks)
- 7 a. Prove that the slope and deflection of a simply supported beam of length L and carrying a uniformly distributed load of W per unit length over the entire length are given by

Slope at the supports = 
$$\frac{WL^2}{24EI}$$
 and Deflection at centre =  $\frac{5}{384} \frac{WL^3}{EI}$ ,

where  $W = Total load = W \times L$ .

(10 Marks)

- b. A beam of length 5m and of uniform rectangular section is simply supported at its ends. It carries a uniformly distributed load of 9kN/m run over the entire length. Calculate the width and depth of the beam if permissible bending stress is 7N/mm<sup>2</sup> and central deflection is not to exceed 1cm. (10 Marks)
- What are the assumptions made in Euler's theory? (03 Marks)
  - Derive an expression for Euler's buckling load for a column with its both ends are fixed. (07 Marks)
  - c. A solid circular shaft is to transmit 300kW at 100rpm. If the shear stress in not to exceed 80N/mm<sup>2</sup>. Find the diameter of the shaft. What percentage in saving in weight would be obtained, if this shaft is replaced by a hollow one, whose internal diameter is equal to 0.8 of the external diameter, the length, the material and the allowable maximum shear stress being the same? (10 Marks)